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JEE (ADVANCED) 2023

QUESTIONS & TEXT SOLUTION

PAPER-1

DATE & DAY: 4th JUNE 2023, SUNDAY

PAPER-1	PAPER-2
Duration: 3 Hrs.	**Duration:** 3 Hrs.
Time: 09:00 - 12:00 IST	**Time:** 14:30 - 17:30 IST

SUBJECT: PHYSICS

REGISTERED & CORPORATE OFFICE (CIN: U80302RJ2007PLC024029):
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TARGET: JEE (Adv.) 2024

VIJAY COURSE

For 12th Passed Students

Course Features*

- Course Duration: **32 Weeks**
- Total No. of Lectures: **533** (P: 178 | C: 177 | M: 178)
- Duration of One Lecture: **1.5 Hrs.** (90 Minutes)
- Classroom Teaching Hours.: **800 Hrs.**
- Testing Duration: **60 Hrs.**
- Total Academic Hours.: **860 Hrs.**

CLASS STARTS
5th & 19th June

AIR 6
JEE (Adv.) 2022
KARTHIKEYA P.

SCHOLARSHIP UPTO 100%
Based on JEE (Advanced) 2023 Score, Scholarship Test (ResoNET) & 12th Board

TARGET: JEE (Main) 2024

AIR 5
JEE (Main) 2023
KAUSHAL V.

SCHOLARSHIP UPTO 100%
Based on JEE (Main) 2023 Score, Scholarship Test (ResoNET) & 12th Board

AJAY COURSE

For 12th Passed Students

Course Features*

- Course Duration: **33 Weeks**
- Total No. of Lectures: **571** (P:1 84 | C: 203 | M: 184)
- Duration of One Lecture: **1.5 Hrs.** (90 Minutes)
- Classroom Teaching Hours.: **857 Hrs.**
- Testing Duration: **33 Hrs.**
- Total Academic Hours.: **890 Hrs.**

CLASS STARTS
5th & 19th June

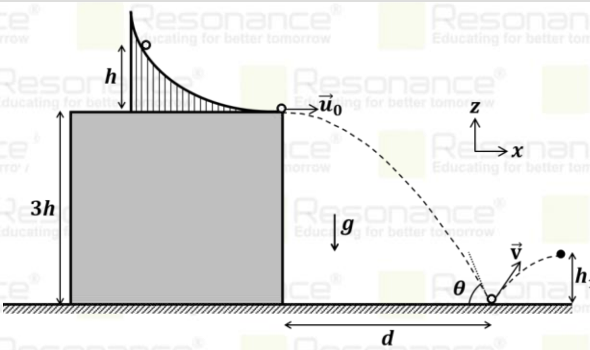
PART : PHYSICS

SECTION 1 (Maximum Marks: 12)

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

  Full Marks : +4 **ONLY** if (all) the correct option(s) is(are) chosen;
  Partial Marks : +3 If all the four options are correct but **ONLY** three options are chosen;
  Partial Marks : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;
  Partial Marks : +1 If two or more options are correct but **ONLY** one option is chosen and it is acorrect option;
  Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
  Negative Marks : −2 In all other cases.
- For example, in a question, if (A), (B) and (D) are the ONLY three options corresponding to correct answers, then
  choosing ONLY (A), (B) and (D) will get +4 marks;
  choosing ONLY (A) and (B) will get +2 marks;
  choosing ONLY (A) and (D) will get +2 marks;
  choosing ONLY (B) and (D) will get +2 marks;
  choosing ONLY (A) will get +1 mark;
  choosing ONLY (B) will get +1 mark;
  choosing ONLY (D) will get +1 mark;
  choosing no option (i.e. the question is unanswered) will get 0 marks; and
  choosing any other combination of options will get −2 marks.

1. A slide with a frictionless curved surface, which becomes horizontal at its lower end, is fixed on the terrace of a building of height 3h from the ground, as shown in the figure. A spherical ball of mass m is released on the slide from rest at a height h from the top of the terrace. The ball leaves the slide with a velocity $\vec{u}_0 - u_0\hat{x}$ and falls on the ground at a distance d from the building making an angle θ with the horizontal. It bounces off with a velocity $\vec{v}$ and reaches a maximum height h_1. The acceleration due to gravity is g and the coefficient of restitution of the ground is $1/\sqrt{3}$. Which of the following statement(s) is(are) correct?



(A) $\vec{u}_0 = \sqrt{2gh}\hat{x}$ (B) $\vec{v} = \sqrt{2gh}(\hat{x} - \hat{z})$ (C) $\theta = 60°$ (D) $d/h_1 = 2\sqrt{3}$

Ans. **(ACD)**

Sol. From energy conservation :

$\frac{1}{2}mu_0^2 = mgh \Rightarrow u_0 = \sqrt{2gh}$ Option (A) is correct

v_0 is the velocity of ball at ground before collision.

$\vec{v}_0 = \sqrt{2gh}\,\hat{i} - \sqrt{2g(3h)}\,\hat{k}$

$= \sqrt{2gh}\,(\hat{i} - \sqrt{3}\,\hat{k})$

$\tan\theta = \frac{v_z}{v_x} = \frac{\sqrt{2g(3h)}}{\sqrt{2gh}} = \sqrt{3}$

$\theta = 60^o$ Option (C) is correct

$\frac{v_z}{(v_0)_z} = \frac{\sqrt{2gh_1}}{\sqrt{2g(3h)}} = \sqrt{\frac{h_1}{3h}} = e = \frac{1}{\sqrt{3}} \Rightarrow h_1 = h$

$d = u_0\sqrt{\frac{2(3h)}{g}} = \sqrt{2gh}\sqrt{\frac{2\times 3h}{g}}$

$d = 2h\sqrt{3}$

$\frac{d}{h_1} = 2\sqrt{3}$ Option (D) is correct

2. A plane polarized blue light ray is incident on a prism such that there is no reflection from the surface of the prism. The angle of deviation of the emergent ray is $\delta = 60°$ (see Figure-1). The angle of minimum deviation for red light from the same prism is $\delta_{min} = 30°$ (see Figure-2). The refractive index of the prism material for blue light is $\sqrt{3}$. Which of the following statement(s) is(are) correct?

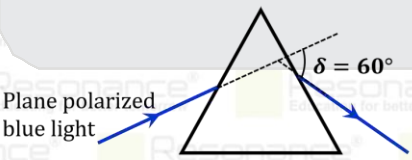


Figure-1

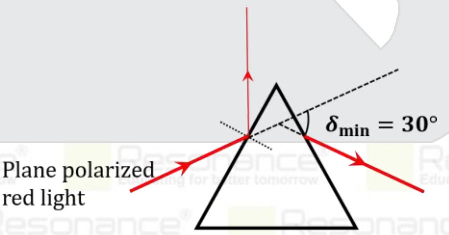


Figure-2

(A) The blue light is polarized in the plane of incidence.

(B) The angle of the prism is 45°.

(C) The refractive index of the material of the prism for red light is $\sqrt{2}$.

(D) The angle of refraction for blue light in air at the exit plane of the prism is 60°.

Ans. **(ACD)**

Sol. For blue light

$\mu = \tan i_p$

$\sqrt{3} = \tan i_p$

$i_p = 60°$

$\delta = i + e - A$

$60 = 60 + e - A$

$e = A$

$\sin 60° = \sqrt{3} \sin r_1$

$\frac{\sqrt{3}}{2} = \sqrt{3} \sin r_1$

$r_1 = 30°$

$r_2 = A - 30°$

$\sqrt{3} \sin (A - 30°) = \sin A$

$\sqrt{3}\left[\sin A \frac{\sqrt{3}}{2} - \cos A \frac{1}{2}\right] = \sin A$

$\frac{3}{2} \sin A - \frac{\sqrt{3}}{2} \cos A = \sin A$

$\frac{-\sqrt{3}}{2} \cos A = -\frac{\sin A}{2}$

$\tan A = \sqrt{3}$

$A = 60°$

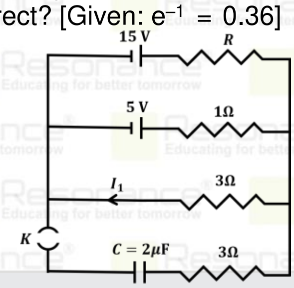
$e = 60°$

For red light

$$= \frac{\sin\left(\frac{A + \delta_{min}}{2}\right)}{\sin\frac{A}{2}} = n_R = \frac{\sin\left(\frac{90}{2}\right)}{\sin 30} = n_R$$

$n = \sqrt{2}$

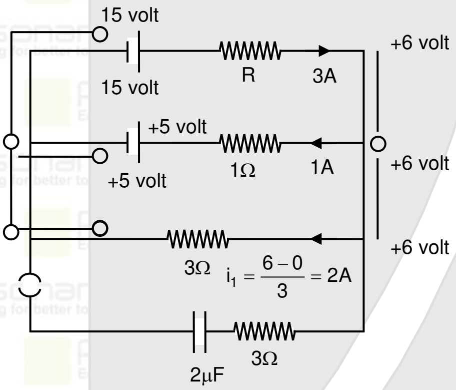
3. In a circuit shown in the figure, the capacitor C is initially uncharged and the key K is open. In this condition, a current of 1 A flows through the 1Ω resistor. The key is closed at time t = t_0. Which of the following statement(s) is(are) correct? [Given: e^{-1} = 0.36]



(A) The value of the resistance R is 3Ω.
(B) For t < t_0, the value of current I_1 is 2 A.
(C) At t = t_0 + 7.2 μs, the current in the capacitor is 0.6 A.
(D) For t → ∞, the charge on the capacitor is 12 μC.

Ans. **(ABCD)**

Sol.

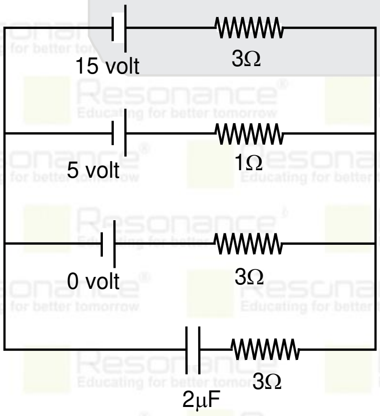


$\frac{x-5}{1} = 1 \Rightarrow x = +6$ volt,

$R = \frac{15-6}{3} = 3\Omega$

$i_1 = \frac{6-0}{3} = 2A$

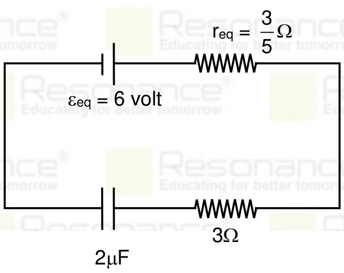
After switching on :



$\varepsilon_{eq} = \frac{\frac{15}{3}+\frac{5}{1}+\frac{0}{3}}{\frac{1}{3}+\frac{1}{1}+\frac{1}{3}} = 6$ volt

$\frac{1}{r_{eq}} = \frac{1}{3}+\frac{1}{1}+\frac{1}{3} \Rightarrow r_{eq} = \frac{3}{5}\Omega$

⇒



(D) Steady state charge on the capacitor

$q = CV = (2\mu)(6) = 12\mu C$

(C) $R_{eq} = \frac{3}{5} + 3 = \frac{18}{5}\ \Omega$, $i_{max} = \frac{\varepsilon_{eq}}{R_{eq}} = \frac{6}{18/5} = \frac{5}{3}$ A

$R_{eq}C = \frac{18}{5} \times 2\Omega = \frac{36}{5}\ \mu$ sec.

$\frac{t}{R_C} = \frac{7.2}{36/5} = 1$

$i(t) = \frac{\varepsilon_{eq}}{R_{eq}} e^{-\frac{t}{R_{eq}C}} = \frac{5}{3} e^{-1} = \frac{5}{3} \times 0.36$

$i = 0.6$ A

SECTION 2 (Maximum Marks: 12)

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correctanswer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:

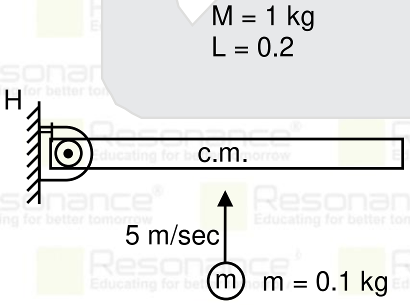
Full Marks : +3 If ONLY the correct option is chosen
Zero Marks : 0 If none of the options is chosen (i.e., the questions is unanswered) ;
Negative Marks : –1 In all other cases.

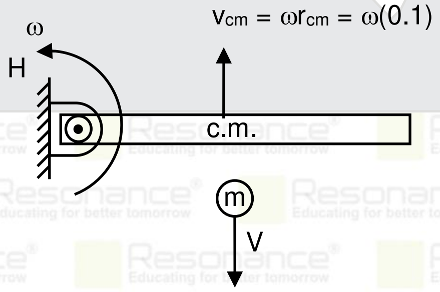
4. A bar of mass M = 1.00 kg and length L = 0.20 m is lying on a horizontal frictionless surface. One end of the bar is pivoted at a point about which it is free to rotate. A small mass m = 0.10 kg is moving on the same horizontal surface with 5.00 ms^{-1} speed on a path perpendicular to the bar. It hits the bar at a distance L/2 from the pivoted end and returns back on the same path with speed v. After this elastic collision, the bar rotates with an angular velocity ω. Which of the following statement is correct?

(A) $\omega = 6.98$ rad s^{-1} and $v = 4.30\ ms^{-1}$
(B) $\omega = 3.75$ rad s^{-1} and $v = 4.30\ ms^{-1}$
(C) $\omega = 3.75$ rad s^{-1} and $v = 10.0\ ms^{-1}$
(D) $\omega = 6.80$ rad s^{-1} and $v = 4.10\ ms^{-1}$

Ans. (A)

Sol.





For the (rod + ball) system :

(i) The angular momentum will remain conserved only about the hinge axis.

About the hinge axis : $L_i = L_f$

$$0 + (0.1)(5)(0.1) = \left(\frac{(1)(0.2)^2}{3}\right)\omega - (0.1)(v)(0.1)$$

$\frac{4\omega}{3} - v = 5$ ...(1)

(ii) $e = \frac{\omega(0.1) + v}{5}$ where e = 1

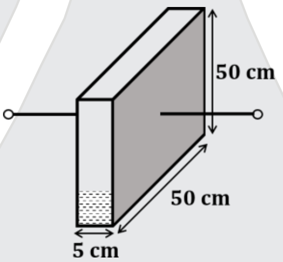
$\frac{\omega}{10} + v = 5$ ...(2)

Solving $\omega = \frac{300}{43} = 6.98$ rad/sec.

v = 4.30 m/sec.

5. A container has a base of 50 cm × 5 cm and height 50 cm, as shown in the figure. It has two parallel electrically conducting walls each of area 50 cm × 50 cm. The remaining walls of the container are thin and non-conducting. The container is being filled with a liquid of dielectric constant 3 at a uniform rate of 250 cm³ s⁻¹. What is the value of the capacitance of the container after 10 seconds?

[Given: Permittivity of free space $\epsilon_0 = 9 \times 10^{-12}\ C^2N^{-1}m^{-2}$, the effects of the non-conducting walls on the capacitance are negligible]



(A) 27 pF (B) 63 pF (C) 81 pF (D) 135 pF

Ans. **(B)**

Sol. Height of water filled at t = 10 sec.

$$h = \frac{250 \times 10}{50 \times 5} = 10\,\text{cm}$$

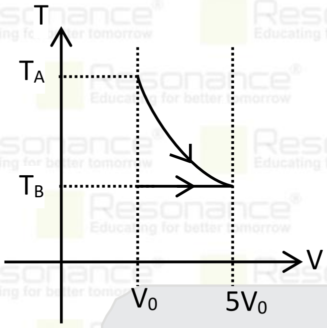
$$C = \frac{\varepsilon_0}{d}[A_1K_1 + A_2K_2] = \frac{9 \times 10^{-12}}{0.05}[0.5 \times 0.1 \times 3 + 0.5 \times 0.4 \times 1] = 63 \times 10^{-12}F$$

6. One mole of an ideal gas expands adiabatically from an initial state (T_A, V_0) to final state (T_f, $5V_0$). Another mole of the same gas expands isothermally from a different initial state (T_B, V_0) to the same final state (T_f, $5V_0$). The ratio of the specific heats at constant pressure and constant volumeof this ideal gas is γ. What is the ratio T_A/T_B?

(A) $5^{\gamma-1}$ (B) $5^{1-\gamma}$ (C) 5^{γ} (D) $5^{1+\gamma}$

Ans. **(A)**

Sol.



$T_A V_0^{\gamma-1} = T_B (5V_0)^{\gamma-1}$

$T_A = 5^{\gamma-1} T_B$

$T_A/T_B = 5^{\gamma-1}$

7. Two satellites P and Q are moving in different circular orbits around the Earth (radius R). The heights of P and Q from the Earth surface are h_P and h_Q, respectively, where $h_P = R/3$. The accelerations of P and Q due to Earth's gravity are g_P and g_Q, respectively. If $g_P/g_Q = 36/25$, what is the value of h_Q?

(A) 3R/5 (B) R/6 (C) 6R/5 (D) 5R/6

Ans. **(A)**

Sol. $\frac{g_P}{g_Q} = \frac{GM/r_P^2}{GM/r_Q^2} = \frac{36}{25}$

$\frac{r_Q}{r_P} = \frac{6}{5} \quad \Rightarrow \quad r_Q = \left(\frac{6}{5}\right)\left(\frac{4R}{3}\right) = \frac{8R}{5} \quad \left(r_Q = h_p + R = \frac{4R}{3}\right)$

$h_Q = \frac{8R}{5} - R = \frac{3R}{5}$

SECTION 3 (Maximum Marks: 24)

- This section contains **SIX (06)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
  Answer to each question will be evaluated according to the following marking scheme :
  Full Marks : + 4 If ONLY the correct integer is entered ;
  Zero Marks : 0 In all other cases.

8. A Hydrogen-like atom has atomic number Z. Photons emitted in the electronic transitions from level n = 4 to level n = 3 in these atoms are used to perform photoelectric effect experiment on a target metal. The maximum kinetic energy of the photoelectrons generated is 1.95 eV. If the photoelectric threshold wavelength for the target metal is 310 nm, the value of Z is______.

[Given: hc = 1240 eV-nm and Rhc = 13.6 eV, where R is the Rydberg constant, h is the Planck's constant and c is the speed of light in vacuum]

Ans. 3

Sol. $\Psi = \frac{hc}{\lambda_{th}} = \frac{1240}{310} = 4$ eV

$KE_{max} = h\upsilon - \Psi$

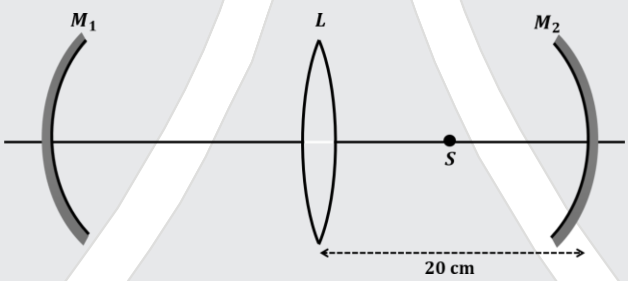
$1.95 = h\upsilon - 4 \Rightarrow h\upsilon = 5.95$ eV

Energy of photon emitted due to electron transition : $\Delta E = 13.6\text{eV } Z^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right)$

$5.95 \text{ eV} = 13.6 \text{ eV } (Z)^2 \left(\frac{1}{(3)^2} - \frac{1}{(4)^2}\right)$

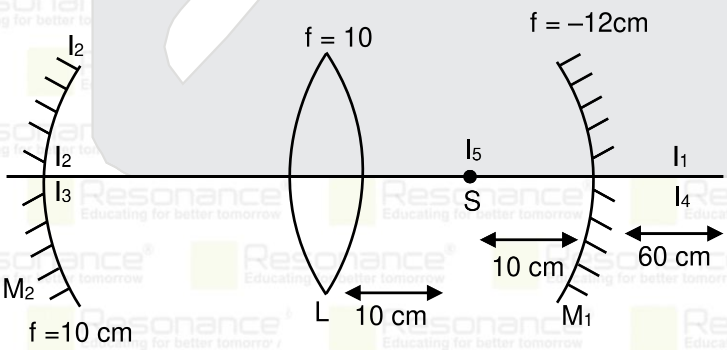
$Z = 3$

9. An optical arrangement consists of two concave mirrors M_1 and M_2, and a convex lens L with a common principal axis, as shown in the figure. The focal length of L is 10 cm. The radii of curvature of M_1 and M_2 are 20 cm and 24 cm, respectively. The distance between L and M_2 is 20 cm. A point object S is placed at the mid-point between L and M_2 on the axis. When the distance between L and M_1 is n/7 cm, one of the images coincides with S. The value of n is____.



Ans. **150 OR 80 OR 220**

Sol. **Case-I**



I^{st} Image

Consider refraction on M_1

$$\frac{1}{V} + \frac{1}{-10} = \frac{1}{-12}$$

$\Rightarrow V = 60$

IInd image

Consider refraction from L

$$\frac{1}{V} - \frac{1}{-80} = \frac{1}{10} \Rightarrow V = \frac{80}{7}$$

It is at the focus of M_2,

so $\frac{80}{7} + 10 = \frac{n}{7}$

n = 150 Ans. **Another cases possible answer is 80 & 220 also correct.**

10. In an experiment for determination of the focal length of a thin convex lens, the distance of the object from the lens is 10 ± 0.1 cm and the distance of its real image from the lens is 20 ± 0.2 cm.The error in the determination of focal length of the lens is n %. The value of n is _____.

Ans. **1**

Sol. $\frac{1}{V} - \frac{1}{U} = \frac{1}{f}$

$$\frac{1}{20} - \frac{1}{-10} = \frac{1}{f}$$

$$f = \frac{20}{3}$$

$$\frac{df}{f^2} = \pm\left[\frac{dv}{V^2} + \frac{du}{U^2}\right] \Rightarrow \frac{df}{f} = \pm f\left[\frac{0.2}{20^2} + \frac{0.1}{10^2}\right]$$

$$\frac{df}{f} = \pm\frac{20}{3}\left[\frac{0.2+0.4}{400}\right] \Rightarrow \frac{df}{f} = \pm\frac{20}{3}\left[\frac{0.6}{400}\right]$$

$$\frac{df}{f} \times 100 = \pm\frac{20}{3}\left[\frac{0.6}{400}\right] \times 100\% = 1\%$$

11. A closed container contains a homogeneous mixture of two moles of an ideal monatomic gas (γ = 5/3) and one mole of an ideal diatomic gas (γ= 7/5). Here, γ is the ratio of the specific heats at constant pressure and constant volume of an ideal gas. The gas mixture does a work of 66 Joule when heated at constant pressure. The change in its internal energy is___Joule.

Ans. **121**

Sol. $n_1 = 2$ $\quad$ $n_2 = 1$

$C_{P_1} = \frac{5}{2}R$ $\quad$ $C_{P_2} = \frac{7}{2}R$

$C_{V_1} = \frac{3}{2}R$ $\quad$ $C_{V_2} = \frac{5}{2}R$

For mixture of gases

$$\gamma = \frac{n_1 C_{P_1} + n_2 C_{P_2}}{n_1 C_{V_1} + n_2 C_{V_2}} = \frac{2\times\frac{5}{2}R + 1\times\frac{7}{2}R}{2\times\frac{3}{2}R + 1\times\frac{5}{2}R} = \frac{17}{11}$$

as gas is heated at constant pressure.

$W = nR\Delta T$

$\Delta U = nC_V\Delta T$

$Q = nC_P\Delta T$

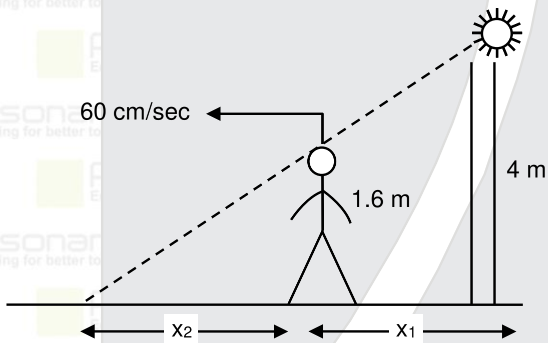
Now, $\frac{\Delta U}{W} = \frac{\Delta U}{Q - \Delta U} = \frac{1}{\frac{Q}{\Delta U} - 1}$ as $Q = \Delta U + W$

$$\frac{\Delta U}{W} = \frac{1}{\frac{C_P}{C_V} - 1} = \frac{1}{\gamma - 1} ; \frac{\Delta U}{W} = \frac{1}{\frac{17}{11} - 1} ; \frac{\Delta U}{66} = \frac{11}{6} ; \Delta U = 121 \text{ J}$$

12. A person of height 1.6 m is walking away from a lamp post of height 4 m along a straight path on the flat ground. The lamp post and the person are always perpendicular to the ground. If the speed of the person is 60 cm s^{-1}, the speed of the tip of the person's shadow on the ground with respect to the person is______cm s^{-1}.

Ans. 40

Sol.

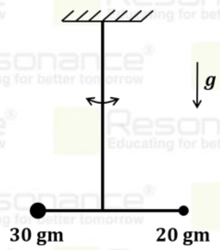


$$\frac{x_1 + x_2}{x_2} = \frac{4}{1.6} = \frac{5}{2} \Rightarrow x_2 = \frac{2}{3} x_1$$

$$\frac{dx_2}{dt} = \frac{2}{3}\frac{dx_1}{dt} \text{ where } \frac{dx_1}{dt} = 60 \text{ cm/sc.}$$

$$\frac{dx_2}{dt} = \left(\frac{2}{3}\right)(60) = 40 \text{ cm/sec.}$$

13. Two point-like objects of masses 20 gm and 30 gm are fixed at the two ends of a rigid massless rodof length 10 cm. This system is suspended vertically from a rigid ceiling using a thin wire attached to its center of mass, as shown in the figure. The resulting torsional pendulum undergoes small oscillations. The torsional constant of the wire is 1.2×10^{-8} N m rad^{-1}. The angular frequency of the oscillations in $n \times 10^{-3}$ rad s^{-1}. The value of n is.



Ans. 10

Sol. $m_{eq} = \frac{m_1 m_2}{m_1 + m_2} = \frac{(20)(30)}{20+30} = 12 \text{ gm} = 12 \times 10^{-3} \text{ kg}$

$I_{cm} = m_{eq} r^2 = (12 \times 10^{-3})(0.1)^2 = 12 \times 10^{-5} \text{ kg.m}^2$

$T = 2\pi\sqrt{\frac{I_{cm}}{C}} = \frac{2\pi}{\omega_n} \Rightarrow \omega_n = \sqrt{\frac{C}{I_{cm}}} = \sqrt{\frac{1.2\times10^{-8}}{12\times10^{-5}}}$

$\omega_n = 10 \times 10^{-3}$ rad/sec.

$= n \times 10^{-3}$ rad/sec. $\Rightarrow n = 10$

SECTION 4 (Maximum Marks: 12)

This section contains **FOUR (04)** Matching List Sets.

- Each set has **ONE** Multiple Choice Question.
- Each set has **TWO** lists: **List-I** and **List-II**.
- **List-I** has **Four** entries (P), (Q), (R) and (S) and **List-II** has **Five** entries (1), (2), (3), (4) and (5).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated **according to the following marking scheme**:

Full Marks : +3 **ONLY** if the option corresponding to the correct combination is chosen;
Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
Negative Marks : −1 In all other cases.

14. List-I shows different radioactive decay processes and List-II provides possible emitted particles. Match each entry in List-I with an appropriate entry from List-II, and choose the correct option.

List-I	**List-II**
(P) ${}^{238}_{92}U \rightarrow {}^{234}_{91}Pa$	(1) one α particle and one β^+ particle
(Q) ${}^{214}_{82}Pb \rightarrow {}^{210}_{82}Pa$	(2) three β^- particles and one α particle
(R) ${}^{210}_{81}Tl \rightarrow {}^{206}_{82}Pb$	(3) two β^- particles and one α particle
(S) ${}^{228}_{91}Pa \rightarrow {}^{224}_{88}Ra$	(4) one α particle and one β^- particles
	(5) one α particle and two β^+ particles

(A) P → 4, Q → 3, R → 2, S → 1
(B) P → 4, Q → 1, R → 2, S → 5
(C) P → 5, Q → 3, R → 1, S → 4
(D) P → 5, Q → 1, R → 3, S → 2

Ans. **(A)**

Sol. **(P)** ${}^{238}_{92}U \rightarrow {}^{234}_{91}Pa + n_1\,{}^{4}_{2}He + n_2\,{}^{0}_{-1}e$

$238 = 234 + 4n_1 \Rightarrow n_1 = 1$

$92 = 91 + 2n_1 - n_2 \Rightarrow n_2 = 1$

(Q) ${}^{214}_{82}Pb \rightarrow {}^{210}_{82}Pb + n_1\,{}^{4}_{2}He + n_2\,{}^{0}_{-1}e$

$214 = 210 + 4n_1 \Rightarrow n_1 = 1$

$82 = 82 + 2n_1 - n_2 \Rightarrow n_2 = 2$

(R) ${}^{210}_{81}T\ell \rightarrow {}^{206}_{82}Pb + + n_1\,{}^{4}_{2}He + n_2\,{}^{0}_{-1}e$

$210 = 206 + 4n_1 \Rightarrow n_1 = 1$

$81 = 82 + 2n_1 - n_2 \Rightarrow n_2 = 3$

(S) ${}^{228}_{91}Pa \rightarrow {}^{224}_{88}Ra + + n_1\,{}^{4}_{2}He + n_2\,{}^{0}_{-1}e$

$228 = 224 + 4n_1 \Rightarrow n_1 = 1$

$91 = 88 + 2n_1 - n_2 = n_2 = -1$

15. Match the temperature of a black body given in List-I with an appropriate statement in List-II, andchoose the correct option. [Given: Wien's constant as 2.9×10^{-3} m-K and $\frac{hc}{e} = 1.24 \times 10^{-6}$ V-m]

List-I	List-II
(P) 2000 K	(1) The radiation at peak wavelength can lead to emission of photoelectrons from a metal of work function 4eV.
(Q) 3000 K	(2) The radiation at peak wavelength is visible to human eye.
(R) 5000 K	(3) The radiation at peak emission wavelength will result in the widest central maximum of a single slitdiffraction.
(S) 10000 K	(4) The power emitted per unit area is 1/16 of thatemitted by a blackbody at temperature 6000 K.
	(5) The radiation at peak emission wavelength can be used to image human bones.

(A) P → 3, Q → 5, R → 2, S → 3
(B) P → 3, Q → 2, R → 4, S → 1
(C) P → 3, Q → 4, R → 2,S → 1
(D) P → 1, Q → 2, R → 5, S → 3

Ans. **(C)**

Sol. $\lambda x T = b$

$$\lambda = \frac{b}{T}$$

$$E = \frac{hc}{\lambda} = \frac{hcT}{b}$$

$$E = \left(\frac{hc}{eb}\right) \times T \text{ eV}$$

$$E = \frac{1.24 \times 10^{-6}}{2.9 \times 10^{-3}} \times T \text{ eV}$$

$E = (0.428 \times 10^{-3} \times T)$ eV

(P) T = 2000 K ⇒ E = 0.856 eV
(Q) T = 3000 K ⇒ E = 1.284 eV
(R) T = 5000 K ⇒ E = 2.14 eV
(S) T = 10000 K ⇒ E = 4.28 eV

16. A series LCR circuit is connected to a 45 sin (ωt) Volt source. The resonant angular frequency of the circuit is 10^5 rad s^{-1} and current amplitude at resonance is I_0. When the angular frequency of the source is $\omega = 8 \times 10^4$ rad s^{-1}, the current amplitude in the circuit is $0.05I_0$. If L = 50 mH, match each entry in List-I with an appropriate value from List-II and choose the correct option.

List-I	List-II
(P) I_0 in mA	(1) 44.5
(Q) The quality factor of the circuit	(2) 18
(R) The bandwidth of the circuit in rad s^{-1}	(3) 400
(S) The peak power dissipated at resonance in Watt	(4) 2250
	(5) 500

(A) P → 2, Q → 3, R → 5, S → 1
(B) P → 3, Q → 1, R → 4, S → 2
(C) P → 4, Q → 5, R → 3, S → 1
(D) P → 4, Q → 2, R → 1, S → 5

Ans. **(B)**

Sol. E = 45 sin(ωt)

$\omega_r L = \frac{1}{\omega_r C}$

$\omega_r^2 = \frac{1}{LC}$

$(10^5)^2 = \frac{1}{50 \times 10^{-3} \times C}$

$10^{10} = \frac{1}{5 \times 10^{-2} C} \Rightarrow c = 2 \times 10^{-9}$ F

at $\omega = 8 \times 10^4$ rad/s

$x_L = \omega L = 8 \times 10^4 \times 50 \times 10^{-3} = 4000\ \Omega$

$x_C = \frac{1}{\omega C} = \frac{1}{8 \times 10^4 \times 2 \times 10^{-9}} = 6250\Omega$

$x = x_C - x_L = 2250\ \Omega$

Also $0.05I_0 = \frac{45}{z}$

$0.05 \times \frac{45}{R} = \frac{45}{z}$

$z = \frac{R}{0.05}$

$\sqrt{R^2 + x^2} = 20\ R$

$R^2 + x^2 = 400R^2$

$\Rightarrow R = 112.6\ \Omega$ (as $x = 2250\Omega$)

(P) $I_0 = \frac{45}{112.6}$ A $= \frac{45 \times 1000}{112.6}$ mA ≈ 400 mA

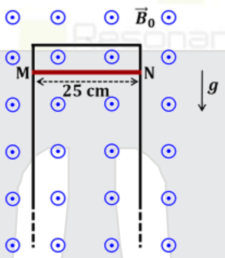
(Q) $Q_{factor} = \frac{\omega_r \times L}{R} = \frac{10^5 \times 50 \times 10^{-3}}{112.6} = 44.4$

(R) B and width = R/L = 2250 rad/s

(S) Peak power at resonance $= \frac{(45)^2}{R} = \frac{(45)^2}{112.6} \approx 18\omega$

17. A thin conducting rod MN of mass 20 gm, length 25 cm and resistance 10Ω is held on frictionless, long, perfectly conducting vertical rails as shown in the figure. There is a uniform magnetic field B_0 = 4T directed perpendicular to the plane of the rod-rail arrangement. The rod is released from rest at time t = 0 and it moves down along the rails. Assume air drag is negligible. Match each quantity in List-I with an appropriate value from List-II, and choose the correct option.

[Given: The acceleration due to gravity g = 10 m s^{-2} and e^{-1} = 0.4]

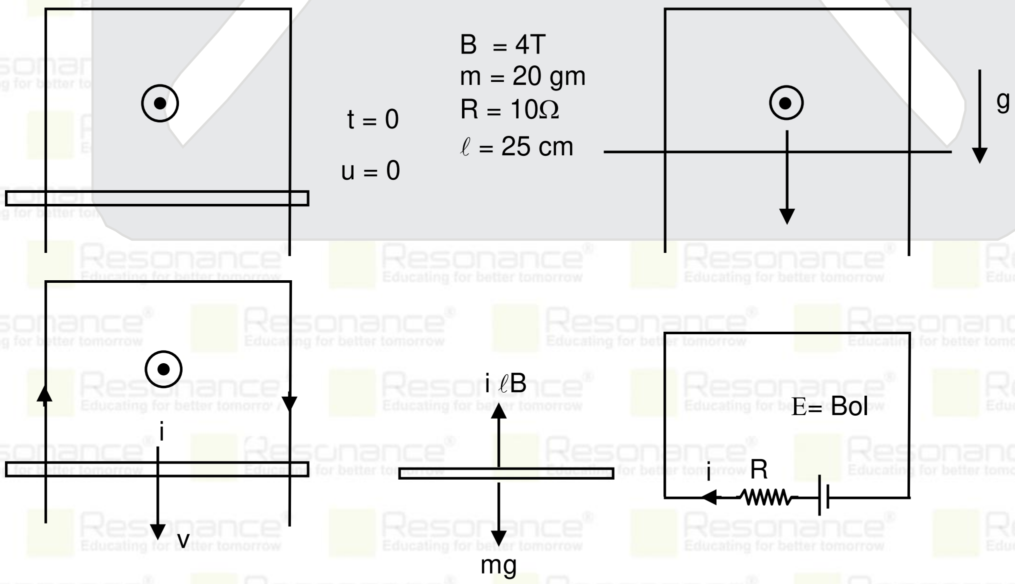


List-I	List-II
(P) At t = 0.2s, the magnitude of the induced emf in Volt	(1) 0.07
(Q) At t = 0.2s, the magnitude of the magnetic force in Newton	(2) 0.14
(R) At t = 0.2s, the power dissipated as heat in Watt	(3) 1.20
(S) The magnitude of terminal velocity of the rod in m s^{-1}	(4) 0.12
	(5) 2.00

(A) P → 5, Q → 2, R → 3, S → 1
(B) P → 3, Q → 1, R → 4, S → 5
(C) P → 4, Q → 3, R → 1, S → 2
(D) P → 3, Q → 4, R → 2, S → 5

Ans. **(D)**

Sol.



$mg - i\ell B - m\dfrac{dv}{dt}$

$B v \ell = iR$

$mg - \left(\dfrac{Bv\ell}{R}\right) B\ell = m\dfrac{dv}{dt}$

$\dfrac{B^2\ell^2}{mR} = \dfrac{1}{20\times10^{-3}\times10} = 5$

$\dfrac{mgR}{B^2\ell^2} - v = \dfrac{mR}{B^2\ell^2}\dfrac{dv}{dt}$

$\dfrac{mgR}{B^2\ell^2} = \dfrac{20\times10^{-3}\times10\times10}{4\times4\times\frac{1}{4}\times\frac{1}{4}} = 2$

$\dfrac{B^2\ell^2}{mR}\int_0^t dt = \int_0^v \dfrac{dv}{\frac{mgR}{B^2\ell^2} - v}$

$5t = -\ln\left[\dfrac{2-v}{2}\right]$

$v = 2\left[1 - e^{-5t}\right]$

for $t = 0.2s$

$v = 2\,(1 - e^{-1})$

$v = 2\,(1 - 04)$

$v = 1.2\ ms^{-1}$

$E = Bv\ell = 4 \times 1.2 \times \dfrac{1}{4} = 1.2\ V$

$i = \dfrac{Bv\ell}{R} = \dfrac{1.2}{10} = 0.12\ A$

$F = mg - i\ell B = 20 \times 10^{-3} \times 10 - 0.12$

$= 0.08\ N$

$P = i^2R = 0.12 \times 0.12 \times 10 = 0.144\ W$

Terminal velocity $v = 2$ for $t = \infty$

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