Resonance®
Educating for better tomorrow

JEE (ADVANCED) 2023

QUESTIONS & TEXT SOLUTION

PAPER-2

DATE & DAY: 4th JUNE 2023, SUNDAY

PAPER-1	PAPER-2
Duration: 3 Hrs.	**Duration:** 3 Hrs.
Time: 09:00 – 12:00 IST	**Time:** 14:30 – 17:30 IST

SUBJECT: PHYSICS

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TARGET: JEE (Adv.) 2024

VIJAY COURSE
For 12th Passed Students

AIR 6
JEE (Adv.) 2022
KARTHIKEYA P.

Course Features*

- Course Duration: **32 Weeks**
- Total No. of Lectures: **533** (P: 178 | C: 177 | M: 178)
- Duration of One Lecture: **1.5 Hrs.** (90 Minutes)
- Classroom Teaching Hours.: **800 Hrs.**
- Testing Duration: **60 Hrs.**
- Total Academic Hours.: **860 Hrs.**

CLASS STARTS
5th & 19th June

SCHOLARSHIP UPTO 100%
Based on JEE (Advanced) 2023 Score,
Scholarship Test (ResoNET) & 12th Board

TARGET: JEE (Main) 2024

AJAY COURSE
For 12th Passed Students

AIR 5
JEE (Main) 2023
KAUSHAL V.

Course Features*

- Course Duration: **33 Weeks**
- Total No. of Lectures: **571** (P:1 84 | C: 203 | M: 184)
- Duration of One Lecture: **1.5 Hrs.** (90 Minutes)
- Classroom Teaching Hours.: **857 Hrs.**
- Testing Duration: **33 Hrs.**
- Total Academic Hours.: **890 Hrs.**

SCHOLARSHIP UPTO 100%
Based on JEE (Main) 2023 Score,
Scholarship Test (ResoNET) & 12th Board

CLASS STARTS
5th & 19th June

PART : PHYSICS

SECTION 1 (Maximum Marks: 12)

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:
  Full Marks   :   +3 If **ONLY** the correct option is chosen;
  Zero Marks   :   0 If none of the options is chosen (i.e. the question is unanswered);
  Negative Marks :   −1 In all other cases.

1. An electric dipole is formed by two charges +q and -q located in x-y plane at (0, 2) mm and (0, −2) mm, respectively, as shown in the figure. The electric potential at point P (100,100) mm due to the dipole is V_0. The charges +q and -q are then moved to the points (−1, 2) mm and (1, −2) mm, respectively. What is the value of electric potential at P due to the new dipole?
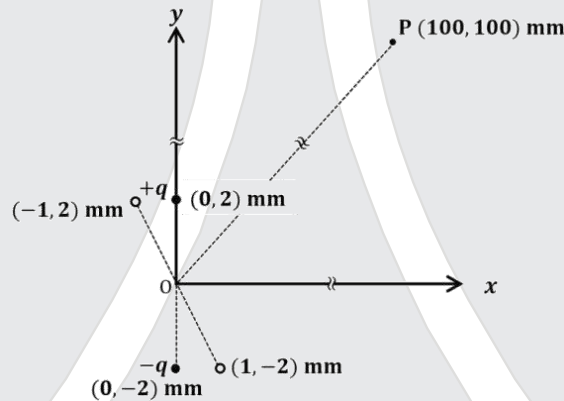
(A) $V_0/4$ (B) $V_0/2$ (C) $V_0/\sqrt{2}$ (D) $3V_0/4$

Ans. **(B)**

Sol. $\vec{p}_1 = q \times 4 \times 10^{-3} \ \hat{j}$

V_{at} (100, 100) mm , $V_0 = \dfrac{K\vec{p}_1.\vec{r}_1}{|\vec{r}_1|^3}$

$V_0 = \dfrac{9\times10^9 \times q\times[4\times10^{-3}\,\hat{j}].(0.1\hat{i}+0.1\hat{j})}{\left(\sqrt{(0.1)^2+(0.1)^2}\right)^3}$

$V_0 = \dfrac{9\times10^9 \times q\times[0.4\times10^{-3}]}{(0.1)^2 \times 2\sqrt{2}}$

Now +q & − q are moved to (–1, 2) mm and (1, – 2) mm

$\vec{p} = q\,[-2\hat{i} + 4\,\hat{j}]\times10^{-3}$

$\vec{r}_1 = 0.1\,\hat{i} + 0.1\,\hat{j}$

$V = \dfrac{9\times10^9(\vec{p}.\vec{r}_1)}{|\vec{r}_1|^3} = \dfrac{9\times10^9 \times q[-0.2+0.4]\times10^{-3}}{\left(\sqrt{(0.1)^2+(0.1)^2}\right)^3}$

$V = \dfrac{9\times10^9 \times q[0.2]\times10^{-3}}{(0.1)^2 \times 2\sqrt{2}} \ \Rightarrow\ V = \dfrac{v_0}{2}$

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2. Young's modulus of elasticity Y is expressed in terms of three derived quantities, namely, the gravitational constant G, Planck's constant h and the speed of light c, as $Y = c^\alpha h^\beta G^\gamma$. Which of the following is the correct option?

(A) $\alpha = 7, \beta = -1, \gamma = -2$ (B) $\alpha = -7, \beta = -1, \gamma = -2$

(C) $\alpha = 7, \beta = -1, \gamma = 2$ (D) $\alpha = -7, \beta = 1, \gamma = -2$

Ans. **(A)**

Sol. $Y = C^\alpha h^\beta G^\gamma$

$$= [LT^{-1}]^\alpha [M^1L^2T^{-1}]^\beta \left[\frac{MLT^{-2}L^2}{M^2} \right]^\gamma$$

$$= [LT^{-1}]^\alpha [M^1L^2T^{-1}]^\beta [M^{-1}L^3T^{-2}]^\gamma$$

$$M^1L^{-1}T^{-2} = M^{\beta-\gamma} L^{\alpha + 2\beta + 3\gamma} T^{-\alpha - \beta - 2\gamma}$$

$\beta - \gamma = 1$ …(1)

$\alpha + 2\beta + 3\gamma = -1$ …(2)

$\alpha + \beta + 2\gamma = 2$ …(3)

Equation (2) – (3)

$\beta + \gamma = -3$

$\beta - \gamma = 1$

—————————

$2\beta = -2$

$\beta = -1$

$\gamma = -2$

$\alpha = 2 - \beta - 2\gamma = 2 + 1 - 2(-2) = 3 + 4 = 7$

3. A particle of mass m is moving in the x-y plane such that its velocity at a point (x, y) is given as $\vec{v} = \alpha(y\hat{x} + y\hat{y})$, where α is a non-zero constant. What is the force $\vec{F}$ acting on the particle?

(A) $\vec{F} = 2m\alpha^2 (x\hat{x} + y\hat{y})$ (B) $\vec{F} = m\alpha^2 (y\hat{x} + 2x\hat{y})$ (C) $\vec{F} = 2m\alpha^2 (y\hat{x} + x\hat{y})$ (D) $\vec{F} = m\alpha^2 (x\hat{x} + 2y\hat{y})$

Ans. **(A)**

Sol. $\vec{v} = \alpha (y\hat{x} + 2x\hat{y})$

$\Rightarrow v_x = \dfrac{dx}{dt} = \alpha y$ and $v_y = \dfrac{dy}{dt} = 2\alpha x$

$\vec{a} = \dfrac{d\vec{v}}{dt} = \alpha \dfrac{dy}{dt}\hat{x} + 2\alpha \dfrac{dx}{dt}\hat{y} = [(\alpha)(2\alpha x) \hat{x} + 2\alpha(\alpha y) \hat{y}]$

$\vec{a} = [(2\alpha^2 x) \hat{x} + 2(\alpha^2 y) \hat{y}]$

$\vec{a} = 2\alpha^2 (x \hat{x} + y \hat{y})$

$\overrightarrow{F_{net}} = m\vec{a} = 2m\alpha^2 (x \hat{x} + y \hat{y})$

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4. An ideal gas is in thermodynamic equilibrium. The number of degrees of freedom of a molecule of the gas is n. The internal energy of one mole of the gas is U_n and the speed of sound in the gas is v_n. At a fixed temperature and pressure, which of the following is the correct option?

(A) $v_3 < v_6$ and $U_3 > U_6$ (B) $v_5 > v_3$ and $U_3 > U_5$ (C) $v_5 > v_7$ and $U_5 < U_7$ (D) $v_6 < v_7$ and $U_6 < U_7$

Ans. **(C)**

**Sol.** $v = \sqrt{\dfrac{\gamma RT}{M_0}}$ where $\gamma = 1 + 2/n$

and $U = \dfrac{nRT}{2}$

If n is more, γ will be less, so v_{sound} will also be less, but the internal energy U will be more.

SECTION 2 (Maximum Marks: 12)

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is (are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks   :   +4 **ONLY** if (all) the correct option(s) is(are) chosen;

Partial Marks   :   +3 If all the four options are correct but **ONLY** three options are chosen;

Partial Marks   :   +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;

Partial Marks   :   +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;

Zero Marks   :   0 If unanswered;

Negative Marks :   −2 In all other cases.

- For example, in a question, if (A), (B) and (D) are the ONLY three options corresponding to correct answers, then

choosing ONLY (A), (B) and (D) will get +4 marks;

choosing ONLY (A) and (B) will get +2 marks;

choosing ONLY (A) and (D) will get +2marks;

choosing ONLY (B) and (D) will get +2 marks;

choosing ONLY (A) will get +1 mark;

choosing ONLY (B) will get +1 mark;

choosing ONLY (D) will get +1 mark;

choosing no option(s) (i.e. the question is unanswered) will get marks and

choosing any other option(s) will get −2 marks.

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5. A monochromatic light wave is incident normally on a glass slab of thickness d, as shown in the figure. The refractive index of the slab increases linearly from n_1 to n_2 over the height h. Which of the following statement(s) is (are) true about the light wave emerging out of the slab?
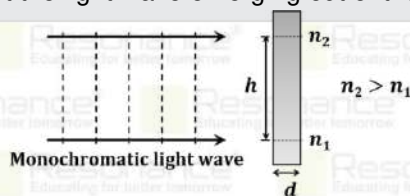
(A) It will deflect up by an angle $\tan^{-1}\left[\dfrac{(n_2^2 - n_1^2)d}{2h}\right]$.

(B) It will deflect up by an angle $\tan^{-1}\left[\dfrac{(n_2 - n_1)d}{h}\right]$

(C) It will not deflect.

(D) The deflection angle depends only on $(n_2 - n_1)$ and not on the individual values of n_1 and n_2.

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Ans. **(BD)**

Sol.
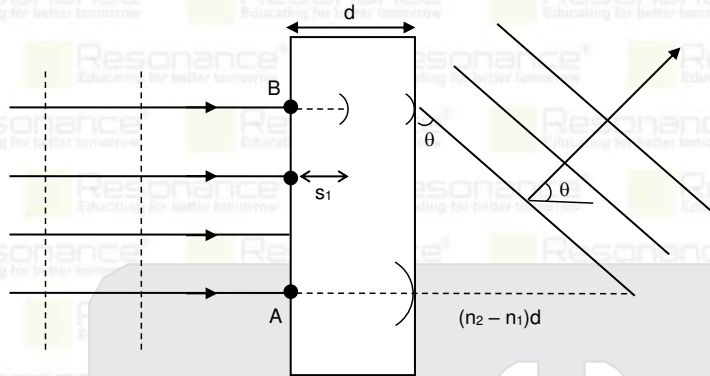
At A wave front reach at the end of slab in time t

$$t = \frac{d}{\frac{c}{n_1}} = \frac{n_1 d}{c}$$

in time t wave front at B travel S_1 ; $\quad S_1 = \frac{c}{n_2} \times \frac{n_1 d}{c} \Rightarrow \frac{d n_1}{n_2}$

when wave front of B reaches at end of slab then further t_1 time take place

$$t_1 = \left(\frac{d - s_1}{c}\right) n_2 = \left[d - \frac{d n_1}{n_2}\right]\frac{n_2}{c} \Rightarrow \frac{d[n_2 - n_1]}{c}$$

in t_1 time wave front at A travel $\Rightarrow S_2$

$S_2 = c t_1 = d [n_2 - n_1]$

$\tan \theta = \frac{(n_2 - n_1)d}{n} \Rightarrow \theta = \tan^{-1} \frac{(n_2 - n_1)d}{h}$ $\qquad$ Ans (BC)

**6.** An annular disk of mass M, inner radius a and outer radius b is placed on a horizontal surface with coefficient of friction μ, as shown in the figure. At some time, an impulse $\mathcal{I}_0 \hat{x}$ is applied at a height h above the center of the disk. If $h = h_m$ then the disk rolls without slipping along the x-axis. Which of the following statement(s) is (are) correct?
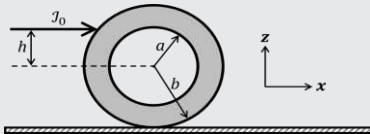
(A) For μ ≠ 0 and a → 0, h_m = b/2.
(B) For μ ≠ 0 and a → b, h_m = b.
(C) For $h = h_m$, the initial angular velocity does **not** depend on the inner radius a.
(D) For μ = 0 and h = 0, the wheel always slides without rolling.

Ans. **(ABCD)**

Sol.
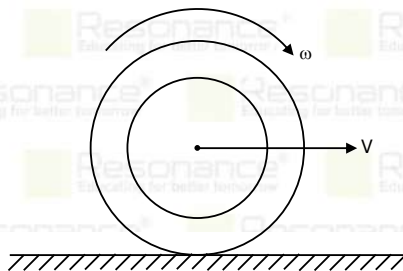
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Angular impulse about CM = ΔL

J_o h = I_{cm} ω

$\omega = \dfrac{J_o h}{I_{cm}}$

Linear impulse = ΔP

$J_o = \Delta$P

$J_o = MV - 0$

$V = \dfrac{J_o}{M}$

As disc is pure rolling $\quad$ V = ωb

$\omega = \dfrac{V}{b}$

$\omega = \dfrac{J_o}{Mb}$

ω is independent of radius a $\qquad$ Ans.(C)

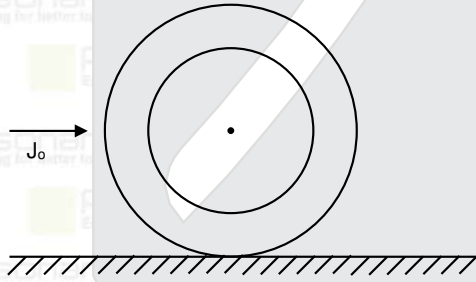If a $\rightarrow$ b then annular disc is ring of radius b

$I_{cm} = Mb^2$

$\therefore$ $\omega = \dfrac{J_o h}{Mb^2}$

$\dfrac{J_o}{Mb} = \dfrac{J_o h}{Mb^2}$

$\qquad$ h = b

$\therefore \qquad h_m = b \qquad\qquad$ Ans.(B)

If h = 0 and μ = 0

as h = 0 $\quad$ $\omega = \dfrac{J_o h}{Mb^2} = 0$ but V = $\dfrac{J_o}{M}$

Wheel always slide without rolling $\qquad$ Ans.(D)

If a $\rightarrow$ 0 then annular disc is disc of radius b

$\therefore \qquad$ Icm = $\dfrac{Mb^2}{2}$

$\omega = \dfrac{J_o h \times 2}{Mb^2}$

$\dfrac{J_o}{Mb} = \dfrac{J_o h \times 2}{Mb^2}$; h = $\dfrac{b}{2}$; $h_m = \dfrac{b}{2}$ $\qquad$ Ans.(A)

7. The electric field associated with an electromagnetic wave propagating in a dielectric medium is given

$\vec{E} = 30 (2\hat{x} + \hat{y}) \sin\left[2\pi\left(5\times10^{14}t - \dfrac{10^7}{3}z\right)\right]$ Vm^{-1} . Which of the following option (s) is (are) correct?

[Given: The speed of light in vacuum, c = 3 × 10^8 m s^{-1}]

(A) $B_x = -2\times10^{-7}\sin\left[2\pi\left(5\times10^{14}t - \dfrac{10^7}{3}z\right)\right]$ Wb m^{-2}

(B) $B_y = 2\times10^{-7}\sin\left[2\pi\left(5\times10^{14}t - \dfrac{10^7}{3}z\right)\right]$ Wb m^{-2}

(C) The wave is polarized in the xy-plane with polarization angle 30° with respect to the x-axis.

(D) The refractive index of the medium is 2.

Ans. **(AD)**

Sol. (A) $\left(B_{x_0}\right) = \dfrac{(E_x)_0}{C} = \dfrac{60}{3\times10^8} = 2\times10^{-7}$

(B) $\left(B_{y_0}\right) = \dfrac{(E_y)_0}{C} = \dfrac{30}{3\times10^8} = 1\times10^{-7}$

(C) Wave is polarized in x–y plane, polarization angle is $\tan^{-1}\left(\dfrac{1}{2}\right)$

(D) Refractive index of medium = $\dfrac{C}{v}$

When $V = \dfrac{w}{R} = \dfrac{5\times10^{14}}{10^7/3} = 15\times10^7 = 1.5\times10^8$ $\qquad \therefore \ \mu = \dfrac{C}{v} = 2$

SECTION 3 (Maximum Marks: 24)

- This section contains **SIX (06)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER.**
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated <u>according to the following marking scheme:</u>

Full Marks : +4 If **ONLY** the correct integer is entered;

Zero Marks : 0 In all other cases.

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8. A thin circular coin of mass 5 gm and radius 4/3 cm is initially in a horizontal xy-plane. The coin is tossed

vertically up (+z direction) by applying an impulse of $\sqrt{\dfrac{\pi}{2}}$ × 10^{-2} N–s at a distance 2/3 cm from its center.

The coin spins about its diameter and moves along the +z direction. By the time the coin reaches back to its initial position, it completes n rotations. The value of n is ____. [Given: The acceleration due to gravity g = 10 m s^{-2}]
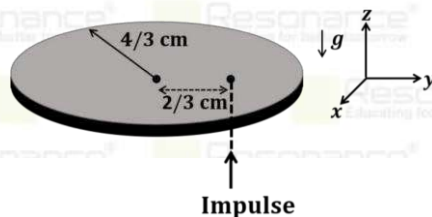

Ans. 30

Sol.

$$J = mv$$

$$Jd = \frac{MR^2}{4}.\omega$$

$$\theta = \omega\left(\frac{2v}{g}\right) = \frac{4Jd}{MR^2}\left(\frac{2v}{g}\right)$$

$$2\pi n = \frac{4J^2}{M^2}\frac{2}{g}\frac{d}{R^2}$$

$$\pi n = \frac{4}{M^2}\times\frac{\pi}{2}\times\frac{10^{-4}}{10}\times\frac{2}{3}10^{-2}\frac{1}{R^2} = \frac{4}{3}\times\frac{10^{-7}\times10^6\times10^4}{25\times\frac{4}{3}.\frac{4}{3}}\times1000 = \frac{3\times1000}{100} = 30$$

9. A rectangular conducting loop of length 4 cm and width 2 cm is in the xy-plane, as shown in the figure. It is being moved away from a thin and long conducting wire along the direction $\frac{\sqrt{3}}{2}\hat{x} + \frac{1}{2}\hat{y}$ with a constant speed v. The wire is carrying a steady current I = 10 A in the positive x-direction. A current of 10 μA flows through the loop when it is at a distance d = 4 cm from the wire. If the resistance of the loop is 0.1Ω, then the value of v is _____ m s⁻¹. [Given: The permeability of free space $\mu_0 = 4\pi \times 10^{-7}$ NA⁻²]
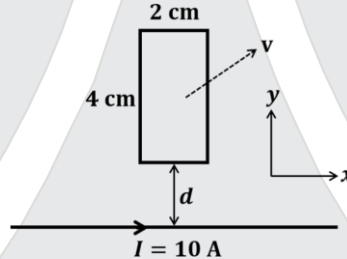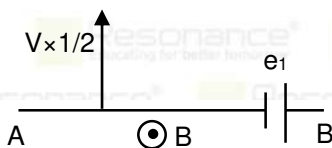

Ans. 04.00

Sol.
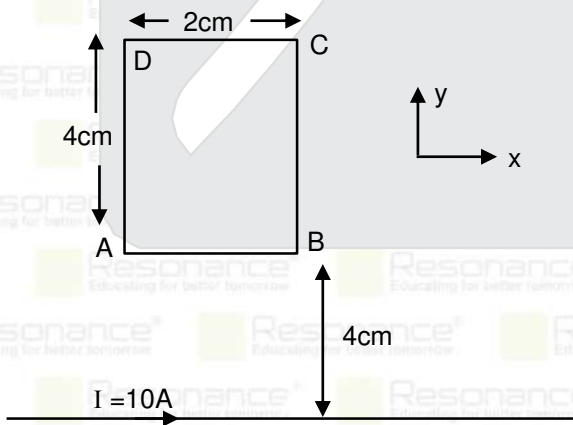
Induced emf in AB = $(\vec{V}\times\vec{B}).\vec{\ell}$

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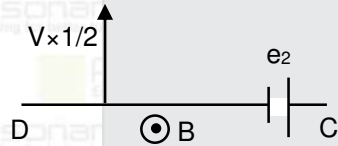
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$$B = \frac{\ell_0 i}{2\pi r} = \frac{4\pi \times 10^{-7}}{2\pi \times 4 \times 10^{-2}} = \frac{1}{2} \times 10^{-4} \, T$$

emf in AB = e_1 = B × $\frac{1}{2}$ × 2 × 10^{-2} × V

$$\Rightarrow \frac{1}{2} \times 10^{-4} \times \frac{1}{2} \times 2 \times 10^{-2} \times V$$
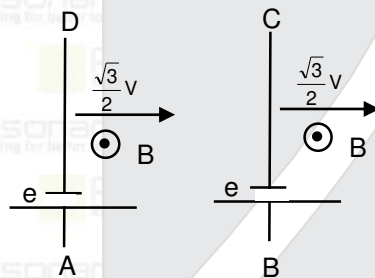
$$\Rightarrow \frac{V}{2} \times 10^{-6} \, Volt$$

Induced emf in CD = e_2 = B × $\frac{1}{2}$ × 2 × 10^{-2} × V

$$\Rightarrow \frac{\mu_0 i}{2\pi(8 \times 10^{-2})} \times \frac{1}{2} \times 2 \times 10^{-2} \times V$$

$$\Rightarrow V \times \frac{1}{4} \times 10^{-6} \, T$$

emf in BC & AD are equal

emf in loop = $e_1 - e_2 + e - e = e_1 - e_2$

$$= V \times \frac{1}{2} \times 10^{-6} - \frac{1}{4} \times 10^{-6} \times V$$

$$= \frac{V}{4} \times 10^{-6}$$

Resistance of loop = 0.1 Ω

Current in loop = I = $\frac{V \times 10^{-6}}{4 \times 0.1} = \frac{10}{4} \times V \, \mu A$

$$\frac{10V}{4} = 10$$

V = 4 m/s

---

10. A string of length 1 m and mass 2×10^{-5} kg is under tension T. When the string vibrates, two successive harmonics are found to occur at frequencies 750 Hz and 1000 Hz. The value of tension T is _____ Newton.

Ans. 05.00

Sol. $\dfrac{V}{2\ell} = 1000 - 750$

$\dfrac{V}{2\ell} = 250$

$V = 2 \times (1) \times 250$

$V = 500$ m/s

$\sqrt{\dfrac{T}{m}} = 500$

$T = (500)^2 \, m = 500 \times 500 \times 2 \times 10^{-5} = 25 \times 2 \times 10^{-1} = 5$ N

11. An incompressible liquid is kept in a container having a weightless piston with a hole. A capillary tube of inner radius 0.1 mm is dipped vertically into the liquid through the airtight piston hole, as shown in the figure. The air in the container is isothermally compressed from its original volume V_0 to $\dfrac{100}{101} V_0$ with the movable piston. Considering air as an ideal gas, the height (h) of the liquid column in the capillary above the liquid level in cm is_____.

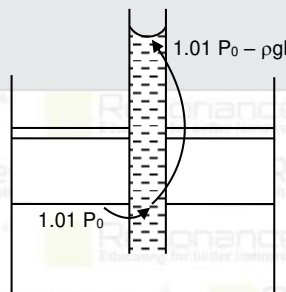[Given: Surface tension of the liquid is 0.075 N m^{-1}, atmospheric pressure is 10^5 N m^{-2}, acceleration due to gravity (g) is 10 ms^{-2}, density of the liquid is 10^3 kg m^{-3} and contact angle of capillary surface with the liquid is zero]
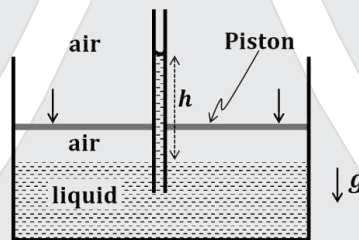
Ans. 25.00

Sol. T = constant

$\Rightarrow$ PV = constant

$P \propto \dfrac{1}{V}$, Volume = $\dfrac{100}{101}$ times, so pressure = $\dfrac{101}{100}$ times = 1.01 times $\Rightarrow P_f = 1.01 \, P_0$

$P_0 - \dfrac{2T}{R} = 1.01 \, P_0 - \rho gh \Rightarrow \rho gh = 0.01 \, P_0 + \dfrac{2T}{R}$

$(10^3)(10) \, h = (0.01)(10^5) + \dfrac{2 \times 0.075}{0.1 \times 10^{-3}} \Rightarrow h = \dfrac{2500}{10^4}$ m = 25 cm.

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12. In a radioactive decay process, the activity is defined as $A = -\dfrac{dN}{dt}$, where N(t) is the number of radioactive nuclei at time t. Two radioactive sources, S_1 and S_2 have same activity at time t = 0. At a later time, the activities of S_1 and S_2 are A_1 and A_2, respectively. When S_1 and S_2 have just completed their 3rd and 7th half-lives, respectively, the ratio A_1/A_2 is _____.

Ans. **16.00**

Sol. n^{th} half life = $\dfrac{A_0}{2^n}$

$$\dfrac{A_1}{A_2} = \dfrac{\dfrac{A_0}{2^3}}{\dfrac{A_0}{2^7}} = 2^4 = 16$$

13. One mole of an ideal gas undergoes two different cyclic processes I and II, as shown in the P-V diagrams below. In cycle I, processes a, b, c and d are isobaric, isothermal, isobaric and isochoric, respectively. In cycle II, processes a', b', c' and d' are isothermal, isochoric, isobaric and isochoric, respectively. The total work done during cycle I is W_I and that during cycle II is W_{II}. The ratio W_I/W_{II} is _____.
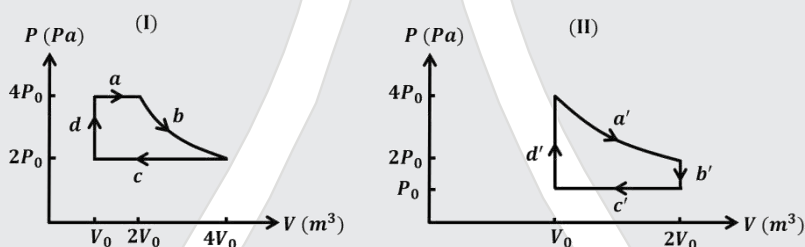
Ans. **02.00**

Sol. $W_I = W_a + W_b + W_c + W_d$

$$= 4P_0(2V_0 - V_0) + (4P_0)(2V_0)\ln\dfrac{4V_0}{2V_0} + 2P_0(V_0 - 4V_0) + 0$$

$$= 8P_0V_0\ln 2 - 2P_0V_0$$

$W_{II} = W_{a'} + W_{b'} + W_{c'} + W_{d'}$

$$= 4P_0V_0\ln\left(\dfrac{2V_0}{V_0}\right) + 0 + P_0(V_0 - 2V_0) + 0$$

$$= 4P_0V_0\ln 2 - P_0V_0$$

$$\dfrac{W_I}{W_{II}} = \dfrac{2}{1} = 2$$

Alternate

$$\dfrac{w_1}{w_2} = \dfrac{4p_0v_0 + 8p_0v_0\ln 2 - 6p_0v_0}{4p_0v_0\ln 2 - p_0v_0}$$

$$= \dfrac{8p_0v_0\ln 2 - 2p_0v_0}{4p_0v_0\ln 2 - p_0v_0} = \dfrac{2(4\ln 2 - 1)}{(4\ln 2 - 1)} = 2$$

SECTION 4 (Maximum Marks: 12)
• This section contains **TWO (02)** paragraphs.
• Based on each paragraph, there are **TWO (02)** questions.
• The answer to each question is a **NUMERICAL VALUE.**
• For each question, enter the correct numerical value of the answer using the mouse and the onscreen virtual numeric keypad in the place designated to enter the answer.
• If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
• Answer to each question will be evaluated <u>according to the following marking scheme:</u> Full Marks   :   +3 If ONLY the correct numerical value is entered in the designated place; Zero Marks   :   0 In all other cases.

PARAGRAPH I

S_1 and S_2 are two identical sound sources of frequency 656 Hz. The source S_1 is located at O and S_2 moves anti-clockwise with a uniform speed $4\sqrt{2}$ m s^{-1} on a circular path around O, as shown in the figure. There are three points P, Q and R on this path such that P and R are diametrically opposite while Q is equidistant from them. A sound detector is placed at point P. The source S_1 can move along direction OP. [Given: The speed of sound in air is 324 m s^{-1}]
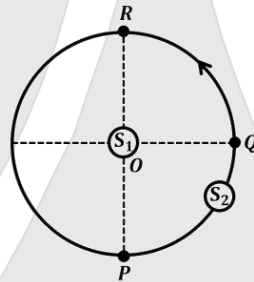
14. When only S_2 is emitting sound and it is at Q, the frequency of sound measured by the detector in Hz is _____.

Ans. 648

Sol.
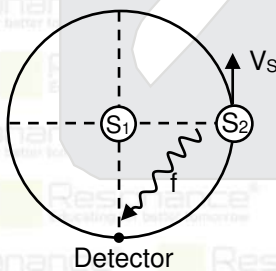
$$f = \frac{V}{V + V_s \cos 45°} \times f_0$$

$$f = \frac{324}{324 + 4} \times 656 = 648$$

15. Consider both sources emitting sound. When S_2 is at R and S_1 approaches the detector with a speed 4 m s^{-1}, the beat frequency measured by the detector is _____ Hz.
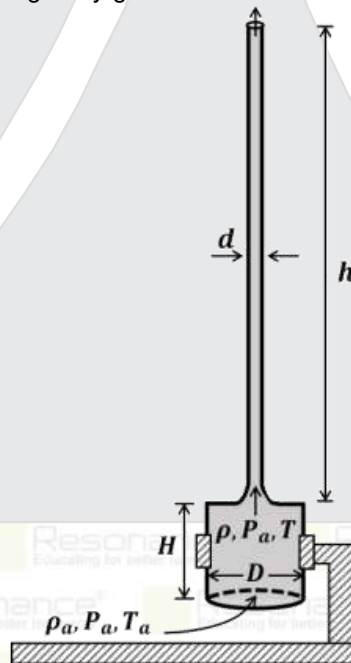
Ans. 8.2

Sol.
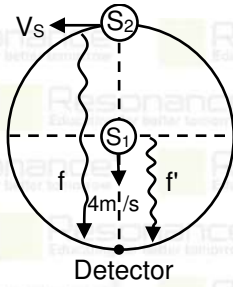
$$f' = \frac{V}{V - V_s} \times f_0$$

$$f' = \frac{324}{324 - 4} \times 656 = 664.2$$

$f_{beats} = f' - f = 664.2 - 656 = 8.2$

PARAGRAPH II

A cylindrical furnace has height (H) and diameter (D) both 1 m. It is maintained at temperature 360 K. The air gets heated inside the furnace at constant pressure P_a and its temperature becomes T = 360 K. The hot air with density ρ rises up a vertical chimney of diameter d = 0.1 m and height h = 9 m above the furnace and exits the chimney (see the figure). As a result, atmospheric air of density ρ_a =1.2 kg m^{-3}, pressure P_a and temperature T_a = 300 K enters the furnace. Assume air as an ideal gas, neglect the variations in ρ and T inside the chimney and the furnace. Also ignore the viscous effects.

[Given: The acceleration due to gravity g = 10 m s^{-2} and π = 3.14]

16. Considering the air flow to be streamline, the steady mass flow rate of air exiting the chimney is _____ gm s^{-1}.

Ans. **60.8 gm/sec.**

Sol.
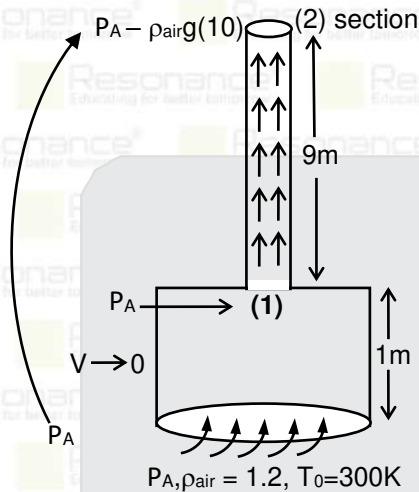
To compare the outer and inner air $\rho = \dfrac{\rho RT}{M_0}$

$\rho \propto \dfrac{1}{T} \Rightarrow \dfrac{\rho_1}{\rho_1} = \dfrac{T_1}{T_2}$

$\dfrac{\rho_1}{1.2} = \dfrac{300}{360} \Rightarrow \rho_{hot} = 1 kg/m^3$

Pressure of outer atmospheric air just above section (2) is

$P_A - \rho_{air}g(10)$, so pressure of hot air coming out of the section (2) will also be $P_A - \rho_{air}g(10)$

Applying Bernoulli's equation between section (1) and (2)

$P_A + \dfrac{1}{2}\rho v_1^2 + \rho gh_1 = P_2 + \dfrac{1}{2}\rho v_2^2 + \rho gh_v$

$P_A + 0 + 0 = \left(P_A - \rho_{air}g(10)\right) + \dfrac{1}{2}\rho_{Hot}v_2^2 + \rho_{Hot}g(9)$

$v_2 = \sqrt{60}\ m/sec$

Rate of mass flow = $\rho_{Hot}AV_2$

$= (1)\left(\dfrac{\pi(0.1)^2}{4}\right)\sqrt{60} = 60.8\,gm/sec.$

17. When the chimney is closed using a cap at the top, a pressure difference ΔP develops between the top and the bottom surfaces of the cap. If the changes in the temperature and density of the hot air, due to the stoppage of air flow, are negligible then the value of ΔP is _____ N m^{-2}.

Ans. 20

Sol. If the chimney is closed, we can apply fluid statics.

$P_{top} = P_A - \rho_{air}g(10)$
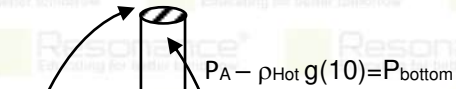
$P_A - \rho_{Hot}\, g(10) = P_{bottom}$

$P_{bottom} - P_{top} = (P_A - \rho_{Hot} + g(10)) - (P_A - \rho_{air}g(10))$

$= (\rho_{air} - P_{Hot})g(10) = (1.2 - 1)(10)(10) = 20$ N/m^2

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